

# Workshop on Methods for Analysis of Fall Chinook Salmon Data

Application of the Classic CJS Mark-Recapture Model

Steven G. Smith  
Northwest Fisheries Science Center  
NOAA Fisheries



- Mark-Recapture Data and “Classic” CJS



- Mark-Recapture Data and “Classic” CJS
- Simple Examples
  - Downstream detections as sample to estimate upstream parameters

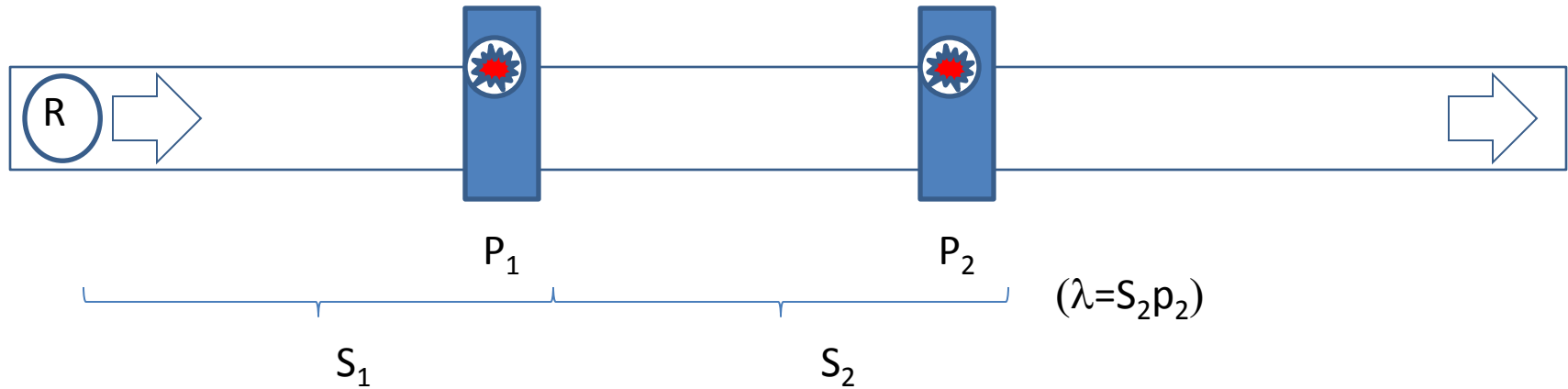
- Mark-Recapture Data and “Classic” CJS
- Simple Examples
  - Downstream detections as sample to estimate upstream parameters
- CJS as Foundation of Estimation of LGR Equivalents

- Mark-Recapture Data and “Classic” CJS
- Simple Examples
  - Downstream detections as sample to estimate upstream parameters
- CJS as Foundation of Estimation of LGR Equivalents
- Model Assumptions
  - Consequences of violations

- Mark-Recapture Data and “Classic” CJS
- Simple Examples
  - Downstream detections as sample to estimate upstream parameters
- CJS as Foundation of Estimation of LGR Equivalents
- Model Assumptions
  - Consequences of violations
  - Relation to data from fall Chinook salmon
    - Protracted migration
    - Changing conditions (esp. spill, transport)
    - Overwintering in reservoirs
    - Undetected passage

# Single-Release of Tagged Individuals

## Two “recapture” occasions



Mark-Recapture Data = Possible PIT-Tag Detection Histories

Detection histories record outcome of series of conditionally independent events.

Histories constitute multinomial sample.

Probability of each history depends on conditional survival and detection probabilities.

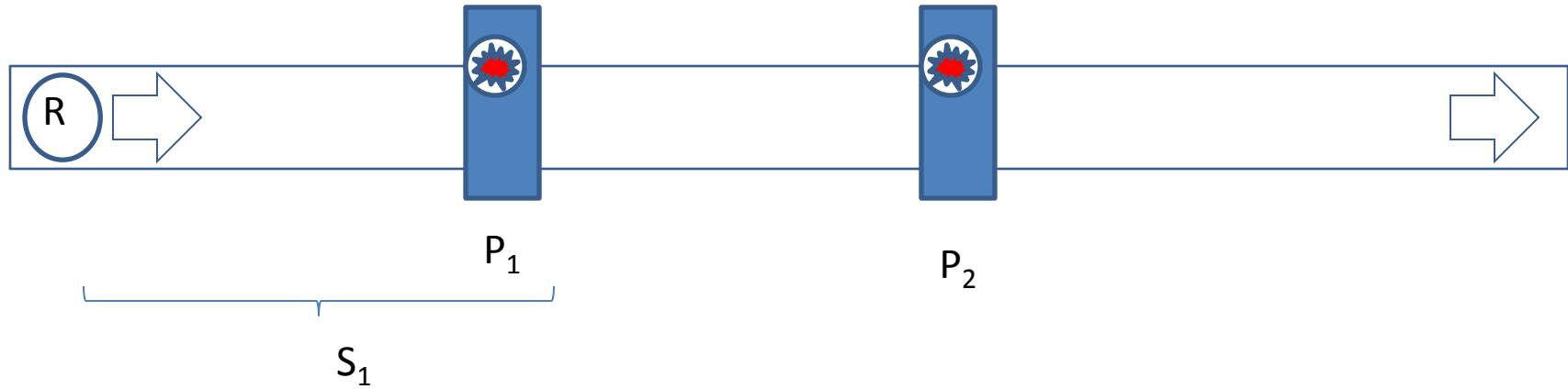
$$111 : S_1 P_1 \lambda$$

$$110 : S_1 P_1 (1 - \lambda)$$

$$101 : S_1 (1 - P_1) \lambda$$

$$100 : (1 - S_1) + S_1 (1 - P_1) (1 - \lambda)$$

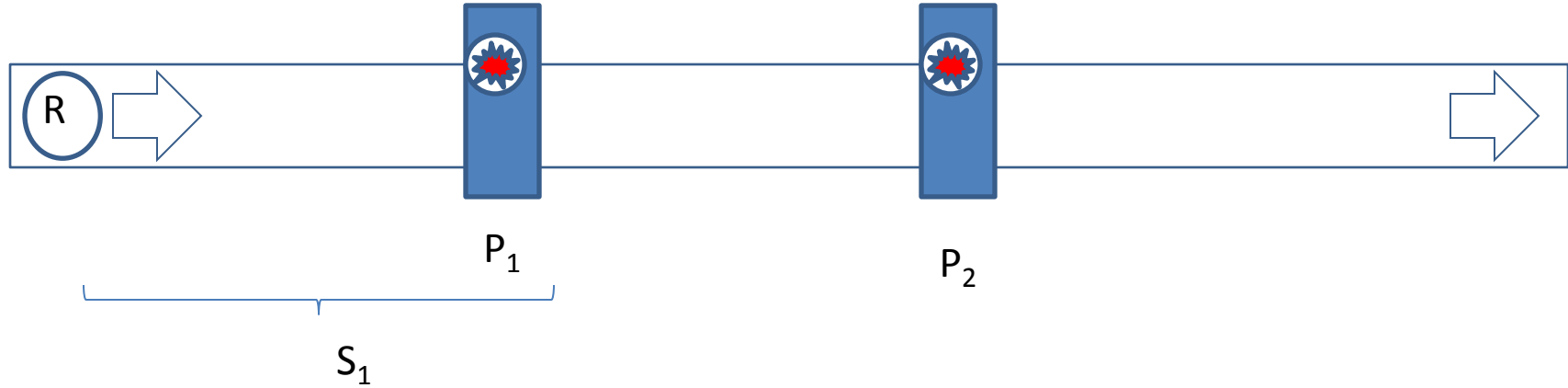
# Two “recapture” occasions – estimation of $S_1$ and $P_1$



Probability of surviving to AND being detected at first dam =  $S_1P_1$

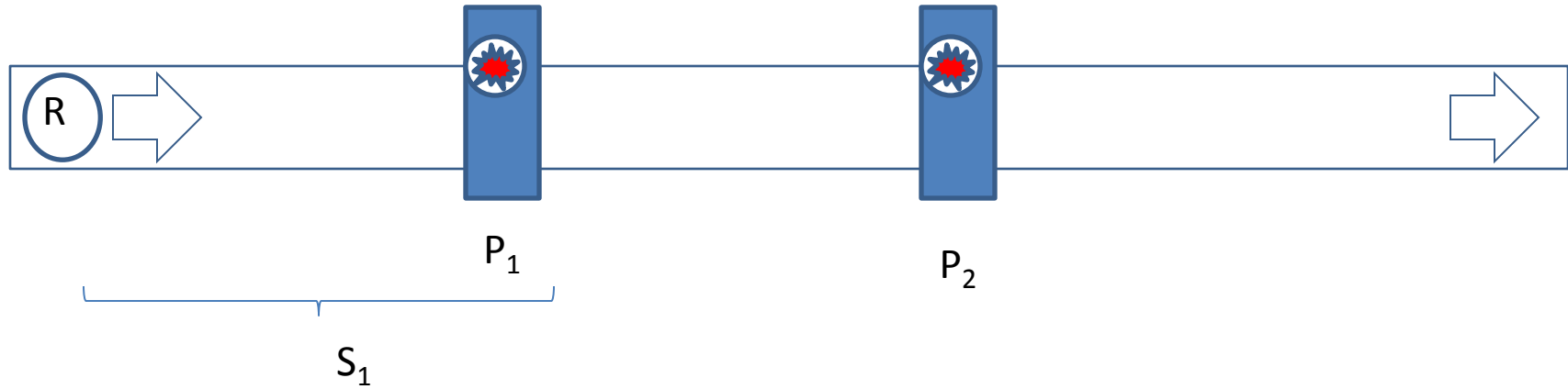
$$\frac{(n_{111} + n_{110})}{R} = \widehat{S_1P_1}$$

# Two “recapture” occasions – estimation of $S_1$ and $P_1$



Given estimate of joint probability of survival and detection, need an estimate of one probability separately to separate.

# Two “recapture” occasions – estimation of $S_1$ and $P_1$

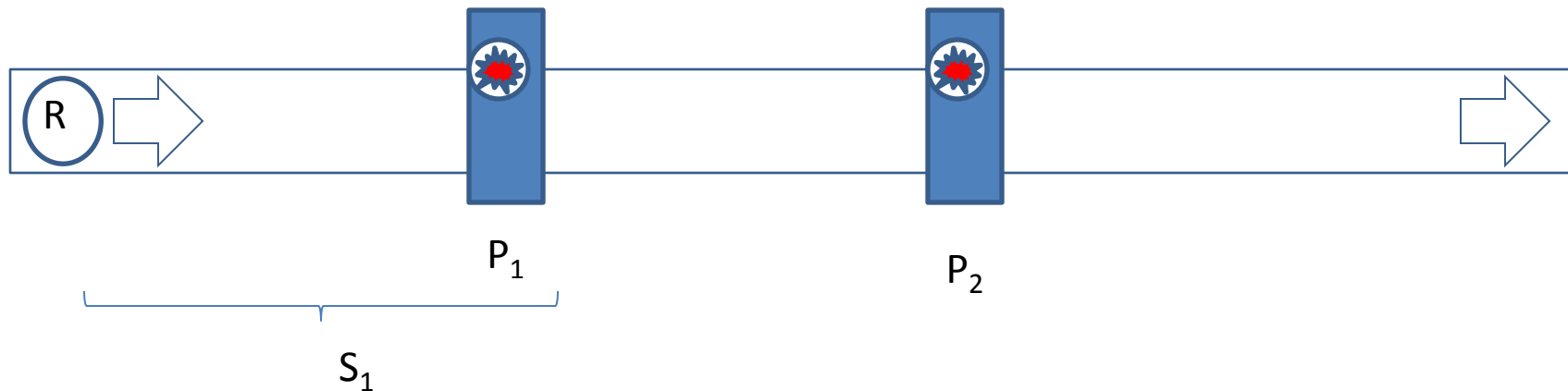


Given estimate of joint probability of survival and detection, need an estimate of one probability separately to separate.

$$\hat{P}_1 = \frac{n_{111} + n_{110}}{(n_{111} + n_{110} + n_{101} + n_{100})}$$

no good because some “100” fish were not alive at dam 1.

## Two “recapture” occasions – estimation of $S_1$ and $P_1$



Given estimate of joint probability of survival and detection, need an estimate of one probability separately to separate.

$$\hat{P}_1 = \frac{n_{111} + n_{110}}{(n_{111} + n_{110} + n_{101} + n_{100})} \text{ no good because some "100" fish were not alive at dam 1.}$$

Fish detected at second dam (111 and 101) constitute a **sample of all fish alive** at dam 1,  
 => sample proportion detected is an estimate of overall probability of detection  
 => detection probability at dam 2 ( $P_2$ ) is a sampling rate

$$\hat{P}_1 = \frac{n_{111}}{(n_{111} + n_{101})}$$

$$\hat{S}_1 = \frac{\widehat{S_1 P_1}}{\hat{P}_1}$$

## Assumptions:

- \* All individuals from a release group alive at head of reach have same probability of survival to end of reach.
- \* All individuals from a release group alive at a detection location have same probability of detection.

## Assumptions:

- \* All individuals from a release group alive at head of reach have same probability of survival to end of reach.
- \* All individuals from a release group alive at a detection location have same probability of detection.

Fish are not balls in an urn – inherent variability among individuals violates these assumptions.

## Assumptions:

- \* All individuals from a release group alive at head of reach have same probability of survival to end of reach.
- \* All individuals from a release group alive at a detection location have same probability of detection.

Fish are not balls in an urn – inherent variability among individuals violates these assumptions.

- Parameter estimates are of *average* probabilities across individuals,



## Assumptions:

- \* All individuals from a release group alive at head of reach have same probability of survival to end of reach.
- \* All individuals from a release group alive at a detection location have same probability of detection.

Fish are not balls in an urn – inherent variability among individuals violates these assumptions.

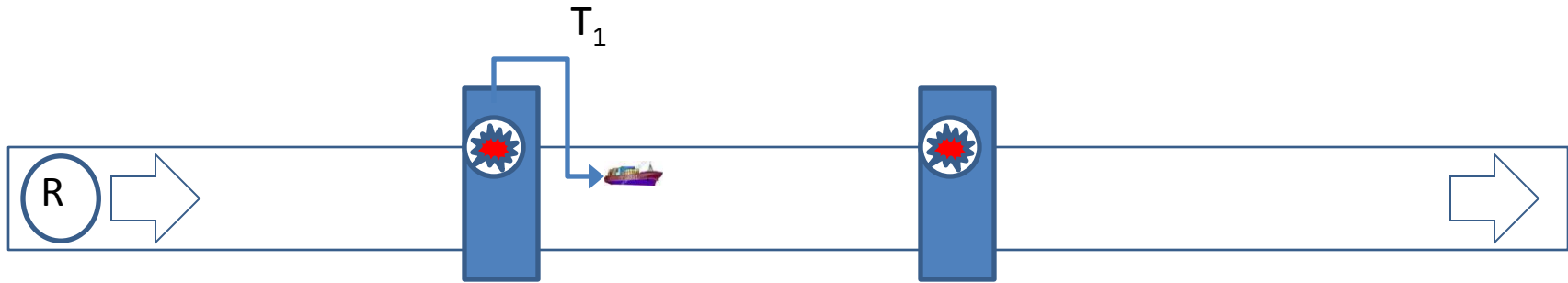
- Parameter estimates are of *average* probabilities across individuals,

BUT, unbiased only if downstream sample is ***representative*** of all alive upstream.

Operations can affect representativeness of downstream sample.



# Effect on sample of fish detected downstream: Transportation



Detection history for fish transported from dam 1: 120

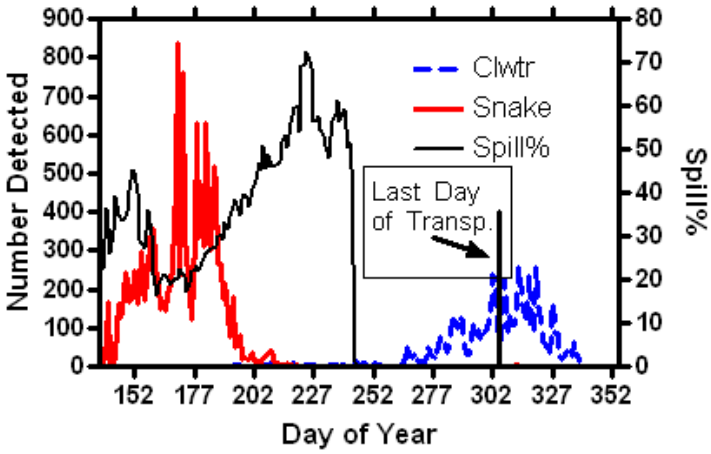
Proportion transported:  $T_1 = \frac{n_{120}}{(n_{111} + n_{110} + n_{120})}$

$$\hat{P}_1 = \frac{n_{111}}{(n_{111} + n_{101}(1 - T_1))}$$

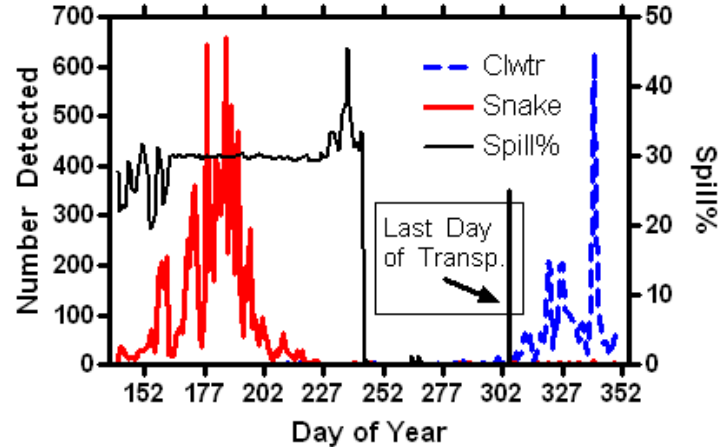
$$\hat{S}_1 = \frac{\overline{S_1 P_1}}{\hat{P}_1}$$

# Potential Issues with Data From PIT-Tagged Fall Chinook Salmon

Detection of Surrogates at Lower Granite 2009

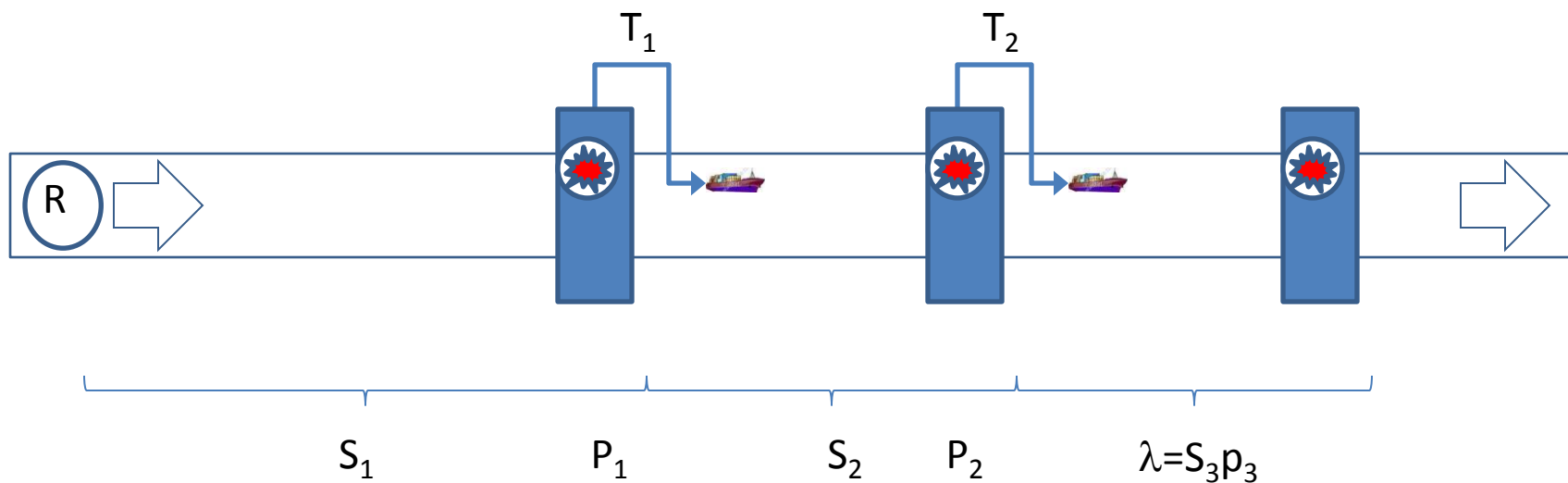


Detection of Surrogates at Little Goose 2009



# Single-Release Experimental Design

## Three “recapture” occasions



### Possible PIT-Tag Detection Histories

1111	1011	1200
1110	1010	1120
1101	1001	1020
1100	1000	

## PIT-Tagged Fall Chinook Salmon Surrogates 2009

	Snake		Clearwater	
	Bypass	Transport	Bypass	Transport
<b>Released</b>	118,870	118,871	45,010	45,006
<b>Detection Histories Based on 2009 Detections</b>				
<b>1111</b>	283	6	390	376
<b>1110</b>	617	23	1,020	917
<b>1101</b>	1,417	104	114	96
<b>1100</b>	4,591	787	1,511	1,253
<b>1011</b>	1,318	116	153	168
<b>1010</b>	3,012	265	527	471
<b>1001</b>	6,665	6,662	62	62
<b>1000</b>	100,242	100,071	40,898	40,925
<b>1200</b>	366	6,371	330	676
<b>1120</b>	56	113	4	7
<b>1020</b>	303	4,353	1	55
<b>Adult Detectors In 2009</b>				
<b>GRA</b>	1	2	5	2
<b>MC1 or MC2</b>	9	6	-	-
<b>Fish Detected in 2010</b>				
<b>Total</b>	47	44	1,205	1,097



## PIT-Tagged Fall Chinook Salmon Surrogates 2009

	Snake	Clearwater
<b>Survival Probability Estimates (Based on 2009 detections only)</b>		
<b>Rel-LGR</b>	0.353 (0.005)	0.107 (0.001)
<b>LGR-LGO</b>	0.764 (0.018)	0.619 (0.010)
<b>Detection Probability Estimates</b>		
<b>LGR</b>	0.175 (0.003)	0.697 (0.007)
<b>LGO</b>	0.177 (0.004)	0.768 (0.011)
<b>Proportion of Detected Transported</b>		
<b>LGR</b>	0.457	0.150
<b>LGO (all)</b>	0.461	0.016
<b>LGO (LGR = 0)</b>	0.497	0.041
<b>LGO (LGR = 1)</b>	0.154	0.004

# Lower Granite Equivalents

## Three “recapture” occasions: LGR, LGO, “below” LGO

- Estimate CJS survival, detection, and transport probabilities.
- Estimate number arriving at LGR:  $\hat{n}_{LGR} = R\hat{S}_1$
- Count “1”s and “2”s at LGR and estimate “0”s:

$$n_1 = n_{1111} + n_{1110} + n_{1101} + n_{1100} + n_{1120} \quad n_2 = n_{1200}$$

$$\hat{n}_0 = \hat{n}_{LGR} - n_1 - n_2$$

- LGR-equivalents = number in each det.hist. category if there were no mortality downstream of LGR:

$$n_{20}^L = n_{1200} \quad \hat{n}_{10}^L = n_1(1 - \hat{P}_2)$$

$$\hat{n}_{12}^L = n_1\hat{P}_2T_2 \quad \hat{n}_{11}^L = n_1\hat{P}_2(1 - T_2) \quad \hat{n}_{00}^L = \hat{n}_0(1 - \hat{P}_2) = C_0$$

$$\hat{n}_{02}^L = \hat{n}_0\hat{P}_2T_2 \quad \hat{n}_{01}^L = \hat{n}_0\hat{P}_2(1 - T_2)$$

# Illustrate Using Parameters of Snake River Surrogates:

Assumptions

Consequences of Violations

Remedies



# Assn: P(Transport) does not depend on previous history

Scenario: LGO transport different for different LGR hist.

LGO (all)	0.461
LGO (LGR = 0)	0.497
LGO (LGR = 1)	0.154

# Assn: P(Transport) does not depend on previous history

Scenario: LGO transport different for different LGR hist.

<b>LGO (all)</b>	0.461
<b>LGO (LGR = 0)</b>	0.497
<b>LGO (LGR = 1)</b>	0.154

	<b>Actual</b>	<b>Estimated</b>
<b>Survival Probabilities</b>		
<b>Rel-LGR</b>	0.353	0.353
<b>LGR-LGO</b>	0.764	0.764
<b>Detection Probabilities</b>		
<b>LGR</b>	0.175	0.175
<b>LGO</b>	0.177	0.177

	<b>Actual</b>	<b>Estimated</b>
<b>LGR Equivalents</b>		
<b>20</b>	6734	6734
<b>12</b>	218	654
<b>02</b>	6103	5667
<b>11</b>	1198	763
<b>10</b>	6577	6577
<b>01</b>	6175	6611
<b>00</b>	57011	57011



# Assn: P(Transport) does not depend on previous history

Scenario: LGO transport different for different LGR hist.

LGO (all)	0.461
LGO (LGR = 0)	0.497
LGO (LGR = 1)	0.154

	Actual	Estimated
<b>Survival Probabilities</b>		
Rel-LGR	0.353	0.353
LGR-LGO	0.764	0.764
<b>Detection Probabilities</b>		
LGR	0.175	0.175
LGO	0.177	0.177

	Actual	Estimated
<b>LGR Equivalents</b>		
20	6734	6734
12	218	218
02	6103	6103
11	1198	1198
10	6577	6577
01	6175	6175
00	57011	57011

## Remedy:

$$\hat{n}_{12}^L = n_1 \hat{P}_2 T_{2.1} \quad \hat{n}_{11}^L = n_1 \hat{P}_2 (1 - T_{2.1})$$

$$\hat{n}_{02}^L = \hat{n}_0 \hat{P}_2 T_{2.0} \quad \hat{n}_{01}^L = \hat{n}_0 \hat{P}_2 (1 - T_{2.0})$$

# Assn: $P_2$ independent of $P_1$ (and $S_2$ , etc.)

## Violated if Downstream sample not representative

1. Size-related detection and/or survival probabilities

# Assn: $P_2$ independent of $P_1$ (and $S_2$ , etc.)

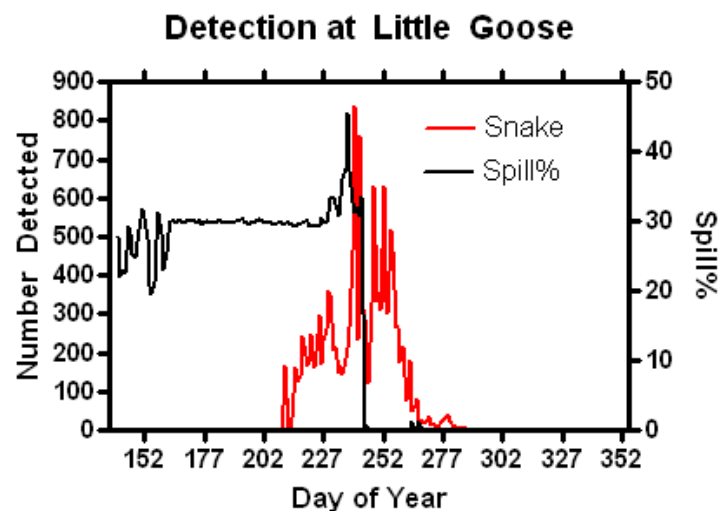
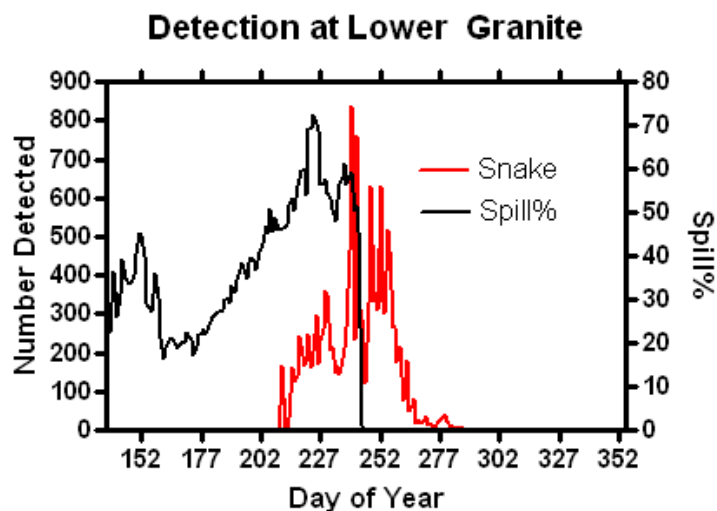
Violated if Downstream sample not representative

1. Size-related detection and/or survival probabilities
2. Behavioral responses to bypass/detection

# Assn: $P_2$ independent of $P_1$ (and $S_2$ , etc.)

Violated if Downstream sample not representative

1. Size-related detection and/or survival probabilities
2. Behavioral responses to bypass/detection
3. Detection probabilities changing at consecutive dams (illustrated below):



# Assn: $P_2$ independent of $P_1$ (and $S_2$ , etc.)

## Scenario: Downstream probability (sampling rate) related to upstream probability/history

- \* Instead of 0.177 detection at LGO for all,  
0.25 for fish detected at LGR  
0.15 for fish not detected at LGR

	Actual	Estimated
<b>Survival Probabilities</b>		
Rel-LGR	0.353	0.311
LGR-LGO	0.764	0.878
<b>Detection Probabilities</b>		
LGR	0.175	0.199
LGO	0.168	0.160

	Actual	Estimated
<b>LGR Equivalents</b>		
20	6,734	6,734
12	308	197
02	5,166	4,722
11	1,691	1,084
10	5,995	6,712
01	5,227	4,778
00	58,896	49,746

# Assn: $P_2$ independent of $P_1$ (and $S_2$ , etc.)

## Scenario: Size effect on detection at consecutive dams

\* Group 1 (“small”): Detection probabilities: 0.200, 0.202

\* Group 2 (“large”): Detection probabilities: 0.150, 0.152

	Actual	Estimated
<b>Survival Probabilities</b>		
Rel-LGR	0.353	0.350
LGR-LGO	0.764	0.767
<b>Detection Probabilities</b>		
LGR	0.175	0.177
LGO	0.177	0.178

	Actual	Estimated
<b>LGR Equivalents</b>		
20	6,734	6,734
12	218	219
02	6,103	6,063
11	1,198	1,204
10	6,577	6,570
01	6,175	6,135
00	57,011	56,295

# Assn: $P_2$ independent of $P_1$ (and $S_2$ , etc.)

## Scenario: Size effect on detection at consecutive dams and survival in consecutive reaches

\* Group 1 (“small”): Detection probabilities: 0.200, 0.206

Survival probabilities: 0.328, 0.739

\* Group 2 (“large”): Detection probabilities: 0.150, 0.152

Survival probabilities: 0.378, 0.786

	Actual	Estimated
<b>Survival Probabilities</b>		
Rel-LGR	0.353	0.353
LGR-LGO	0.764	0.766
<b>Detection Probabilities</b>		
LGR	0.175	0.174
LGO	0.177	0.176

	Actual	Estimated
<b>LGR Equivalents</b>		
20	6,666	6,666
12	218	215
02	6,103	6,064
11	1,198	1,179
10	6,577	6,519
01	6,175	6,136
00	57,012	57,052

# Assn: $P_2$ independent of $P_1$ (and $S_2$ , etc.)

Violated if Downstream sample not representative

1. Size-related detection probabilities
2. Behavioral responses to bypass/detection
3. Detection probabilities changing at consecutive dams

## Remedies

1. Model detection probability as function of size (not solved for LGR equivalents)
- 2, 3(?). Estimate different detection probability at dam 2 for detected and not detected at dam 1



**Fish overwinter in reservoirs.**

**Scenario: 10% of fish spend winter in LGR reservoir, then migrate downstream monitored the following spring**



# Fish overwinter in reservoirs.

**Scenario: 10% of fish spend winter in LGR reservoir, then migrate downstream monitored the following spring**

Pooling Subyearling and Yearling Data		
	Actual	Estimated
<b>LGR Equivalents</b>		
<b>20</b>	6,495	6,495
<b>12</b>	220	213
<b>02</b>	5,559	5,659
<b>11</b>	1,210	1,170
<b>10</b>	6,281	6,328
<b>01</b>	5,919	5,726
<b>00</b>	52,308	52,106

Using Subyearling Data Only		
	Actual	Estimated
<b>LGR Equivalents</b>		
<b>20</b>	6,060	6,060
<b>12</b>	196	196
<b>02</b>	5,493	5,493
<b>11</b>	1,079	1,079
<b>10</b>	5,920	5,920
<b>01</b>	5,557	5,557
<b>00</b>	51,310	51,310



# Fish overwinter in reservoirs.

**Scenario: 5% of fish that enter any reservoir as a subyearling remain there until following spring, then migrate monitored the following spring**

Pooling Subyearling and Yearling Data		
	Actual	Estimated
LGR Equivalents		
20	6,614	6,614
12	226	217
02	5,693	5,912
11	1,244	1,192
10	6,383	6,444
01	6,589	5,981
00	54,256	54,389

Using Subyearling Data Only		
	Actual	Estimated
LGR Equivalents		
20	6,397	6,397
12	197	207
02	5,508	5,798
11	1,028	1,139
10	5,640	6,249
01	5,294	5,866
00	48,880	54,161



# Fish overwinter in reservoirs; some migrate unmonitored.

**Scenario: 5% of fish that enter any reservoir as a subyearling remain there until bypass systems are dewatered.**

**50% of these migrate while detection is not possible.**

<b>Pooling Subyearling and Yearling Data</b>		
	<b>Actual</b>	<b>Estimated</b>
<b>LGR Equivalents</b>		
<b>20</b>	6,506	6,506
<b>12</b>	211	212
<b>02</b>	5,601	5,855
<b>11</b>	1,136	1,155
<b>10</b>	6,011	6,346
<b>01</b>	5,942	5,923
<b>00</b>	51,568	54,265

<b>Using Subyearling Data Only</b>		
	<b>Actual</b>	<b>Estimated</b>
<b>LGR Equivalents</b>		
<b>20</b>	6,397	6,397
<b>12</b>	197	207
<b>02</b>	5,508	5,798
<b>11</b>	1,028	1,139
<b>10</b>	5,640	6,249
<b>01</b>	5,294	5,866
<b>00</b>	48,880	54,161

